

Normalization

Why Normalize?



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Input Normalization



For images, compute mean and standard deviation for each channel – that is, one red mean, one blue mean, and one green mean.

Vanishing / Exploding Gradients



Normalization



Batch Normalization



Batch Normalization

- Keeps the activation magnitudes in check
- Deals with badly scaled weights
- Mixes gradient information between inputs
 - Mitigated by large batches

 $\mathbf{x} \in \mathbb{R}^{B \times C \times H \times W}$ $\mathbf{x}_{i,c,j,k} \rightarrow \infty$ $\mu_c \rightarrow \infty \quad \sigma_c \rightarrow \infty$

BatchNorm at Test Time

• Usually we don't test on a batch of data.

• Keep a running average of the mean and standard deviation during training, then save those values.

Layer Normalization

- Same as BatchNorm, but we compute statistics per input rather than per channel.
- Prevents cross-talk.
- Training and testing are the same.
- In practice, works well for sequence models but not in computer vision.

 $\mathbf{x} \in \mathbb{R}^{B \times C \times H \times W}$

$$\mu_i = \frac{1}{CHW} \sum_{c,j,k} \mathbf{x}_{i,c,j,k}$$

$$\sigma_i^2 = \frac{1}{CHW} \sum_{c,j,k} \left(\mathbf{x}_{i,c,j,k} - \boldsymbol{\mu}_i \right)^2$$

Instance Normalization

- Compute statistics per input and per channel
 - Sum over *only* spatial locations
- Statistics are unstable
- Not so good in recognition
- Works okay for image generation and computer graphics

 $\mathbf{x} \in \mathbb{R}^{B \times C \times H \times W}$

$$\mu_{i,c} = \frac{1}{HW} \sum_{j,k} \mathbf{x}_{i,c,j,k}$$
$$\sigma_{i,c}^2 = \frac{1}{HW} \sum_{j,k} \left(\mathbf{x}_{i,c,j,k} - \mu_{i,c} \right)^2$$

Group Normalization

- Compute statistics over groups of channels
 - Between instance normalization and layer normalization
- More flexible than layer normalization, more stable than instance normalization.

 $\mathbf{x} \in \mathbb{R}^{B \times C \times H \times W}$ S = |C/G| $\mu_{i,g} = \frac{1}{SHW} \sum_{i,k} \sum_{c=S(q-1)}^{Sg-1} \mathbf{x}_{i,c,j,k}$ $\sigma_{i,g}^{2} = \frac{1}{SHW} \sum_{i,k} \sum_{c=S(q-1)}^{Sg-1} (\mathbf{x}_{i,c,j,k} - \mu_{i,g})^{2}$

Summary

Batch normalization



Instance normalization



Layer normalization





Group normalization



Normalization in Practice



- No bias needed in Conv
- Activations are zero mean
 - ReLU will zero out half of activations
- Learn a scale and bias parameter in the normalization layer (affine=True)

- Scale and bias in the normalization layer are optional (affine=False).
- Conv is unchanged

NOTE: Do not normalize after linear layers (statistical estimates are too unstable)